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PAPER

# Floating-Point Multiplier with Concurrent Error Detection Capability by Partial Duplication

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**SUMMARY** A floating-point multiplier with concurrent error detection capability by partial duplication is proposed. It uses a truncated multiplier for checking of the significand (mantissa) multiplication instead of full duplication. The proposed multiplier can detect any erroneous output with error larger than one unit in the last place (1 ulp) of the significand, which may be overlooked by residue checking. Its circuit area is smaller than that of a fully duplicated one. Area overhead of a single-precision multiplier is about 78% and that of a double-precision one is about 65%.

**key words:** concurrent error detection, floating-point multiplier, duplication, truncated multiplier

## 1. Introduction

As aggressive scaling continues to push technology into smaller feature sizes, various design robustness concerns, such as faults by degradation [1]–[3] and soft errors due to particle hits [4], continue to arise. Circuits with concurrent error detection capability are crucial for development of reliable systems. In this paper, we propose a new floating-point multiplier which can detect any erroneous output with magnitude of error larger than one unit in the last place (1 ulp) of the significand (mantissa) by partial duplication. It works appropriately with any rounding mode defined in IEEE 754 floating-point standard [5].

For designing a reliable floating-point circuit, duplication and residue checking [6] have been used. Some processors which use full duplication for arithmetic units were reported [7], [8]. Though floating-point multipliers using full duplication achieve high capability of error detection, they have large area overhead. Reliable floating-point arithmetic units with residue checking were proposed [9] and selection of the modulus for residue checking in IBM processors was discussed in [10]. Though floating-point multipliers using residue checking can achieve high error detection ratio with smaller area overhead, they may overlook erroneous results with large magnitude of error, which is a multiple of the modulus. Furthermore, residue generation during residue checking is timing-critical because the residue needs to be generated after calculation of a result. Full duplication and residue checking are generic methods for basic arithmetic

operations, and they utilize and consider little of the nature of floating-point arithmetic operation. Reliable floating-point arithmetic circuits utilizing methods other than full duplication and residue checking were proposed [11]–[14], but, to the best of our knowledge, are not actually used.

Recently, reduced precision checking is proposed for floating-point addition and floating-point multiplication in [12] and [13], respectively. The technique uses a small significand adder or a small significand multiplier for checking of the result. It mainly considers detection of very large errors, and does not treat rounding which is specific to floating-point arithmetic. Error detection ratio based on this technique reported in [13] is very low as the authors have described. The multiplier based on the method will be used for applications which need to detect only very large errors. The potential applications are different from ones of the multiplier to be proposed and ones of the traditional duplication or residue checking.

The floating-point multiplier to be proposed is based on the proven duplication method and utilizes the nature of floating-point arithmetic. The multiplier consists of a circuit for normal calculation and a circuit for checking as well as a checker which compares the outputs of the two circuits. The calculation sub-circuits of the sign bit and the exponent are duplicated. For the circuit for checking, a truncated multiplier is used for significand calculation instead of a full multiplier. The proposed floating-point multiplier is smaller than one using full duplication because a truncated multiplier sums up only about upper half of partial product bits. The area overhead of the proposed single-precision multiplier and that of the double-precision one are estimated at 78% and 65%, respectively. The floating-point multiplier detects any erroneous output with magnitude of error larger than 1 ulp, which may be overlooked by residue checking.

The proposed multiplier is suitable for applications which need reliability and tolerate small error. For examples, media processing, such as video and image processing, and calculation of a neuron's output in a neural network tolerate small error. Though the calculation of those applications tolerates small error, large error might lead to an incorrect result. Media processing and neural networks are used in various applications such as pedestrian detection from camera images [15], and recognition of the scene [16] for automotive safety or autonomous driving of cars. Reliability is crucial for automotive applications, and the proposed multiplier is useful for those applications.

This paper is organized as follows. In the next sec-

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tion, we describe floating-point multiplication and notations used in this paper. In Sect. 3, we propose a partially duplicated floating-point multiplier. In Sect. 4, we evaluate the proposed multiplier and compare it with designs using full duplication and ones using residue checking. In Sect. 5, we conclude this paper.

## 2. Floating-Point Multiplication

We consider IEEE 754 binary floating-point multiplication. In IEEE 754 standard, a binary floating-point number  $X$  consists of a sign bit  $x_s$ , an exponent  $X_e$ , and a fraction part of significand  $X_m$ . The bit width of the exponent is 8-bit for a single-precision number, and 11-bit for a double-precision number. The bit width of the fraction part of significand is 23-bit and 52-bit, respectively. We represent the bit width of the fraction part of significand by  $l$ . We consider multiplication of normalized numbers. A normalized floating-point number  $X$  represents  $(-1)^{x_s} \times [1.X_m] \times 2^{X_e - bias}$ .  $bias$  is 127 for single-precision, and 1023 for double-precision.

We let the multiplicand, the multiplier, and the resultant product be  $X$ ,  $Y$ , and  $Z$ , respectively. The sign bit and the exponent of  $Z$  are calculated as follows:

$$\begin{aligned} z_s &= x_s \oplus y_s \\ Z_e &= X_e + Y_e - bias + \delta \end{aligned}$$

where  $\delta$  is the increment from the significand calculation, and is either 1 or 0. Let the product of the significands  $[1.X_m] \times [1.Y_m]$  be  $U (= [u_{-1}u_0.u_1 \dots u_{2l}])$ .  $U$  is normalized as

$$V = \begin{cases} [1.u_0 \dots u_{l-1}] & (\text{if } u_{-1} = 1) \\ [1.u_1 \dots u_l] & (\text{otherwise}). \end{cases} \quad (1)$$

After the normalization, rounding is performed by adding rounding bit  $r$  to the least significant position of  $V$ , where  $r$  is either 1 or 0. We represent the result of rounding  $V + r \times 2^{-l}$  as  $W (= [w_{-1}w_0.w_1 \dots w_l])$ . The resultant fraction part of the significand is obtained as

$$Z_m = [.w_1 \dots w_l].$$

The increment  $\delta$  is 1 when  $w_{-1}$  or  $u_{-1}$  is 1.  $\delta$  is 0, otherwise. Note that no special operation is necessary when  $W$  is  $[10.0 \dots 0]$  because all the bits other than  $w_{-1}$  are 0.

In IEEE 754 standard, four rounding modes, i.e., Round ties to even, Round toward positive, Round toward negative and Round toward zero, are defined for binary operations. For Round toward zero, rounding bit  $r$  is 0. For the other modes, it is obtained as follows.

- Round ties to even

$$r = \begin{cases} u_l \wedge (u_{l-1} \vee u_{l+1} \vee st) & (\text{if } u_{-1} = 1) \\ u_{l+1} \wedge (u_l \vee st) & (\text{otherwise}) \end{cases}$$

Here, sticky bit  $st$  is  $u_{l+2} \vee u_{l+3} \vee \dots \vee u_{2l}$ .

- Round toward positive and round toward negative

$$r = \begin{cases} pol \wedge (u_l \vee u_{l+1} \vee st) & (\text{if } u_{-1} = 1) \\ pol \wedge (u_{l+1} \vee st) & (\text{otherwise}) \end{cases}$$

Here,  $pol$  is  $\bar{z}_s$  for round toward positive or  $z_s$  for round toward negative.

## 3. Floating-Point Multiplier with Concurrent Error Detection Capability by Partial Duplication

We propose a floating-point multiplier which can detect any erroneous output with magnitude of error larger than 1 ulp.

### 3.1 Overall Structure

Figure 1 shows a block diagram of the proposed floating-point multiplier. The multiplier consists of three parts: the normal calculation circuit, the calculation circuit for checking, and the checker. In the figure, the left-half is for normal calculation and the right-half is for checking. We use duplication for the sub-circuit for the sign bit and the sub-circuit for the exponent because they are much smaller than the circuit for the significand. We use a special significand calculation circuit for checking instead of full duplication. The checker compares the normal result with the output from the circuit for checking.

### 3.2 Significand Calculation Circuit for Checking

We focus on the significand calculation circuit for checking. For the significand calculation circuit for checking, we use a truncated multiplier. The significand calculation circuit for checking is smaller than the normal significand calculation circuit because a truncated multiplier sums up only upper about half of partial product bits. The output from the truncated multiplier is normalized, rounded and then, adjusted by comparing its least significant bit with that of the result from the normal significand calculation circuit.

Figure 2 shows a block diagram of the significand calculation circuit for checking. It receives  $X_m$  and  $Y_m$ , and the least significant bit of the normal significand result  $w_l$ . It outputs fraction part of significand  $Z'_m$  and increment  $\delta'$  for checking. The significand calculation circuit consists of a truncated multiplier, a normalizer, a rounding bit generator, an incrementer, an adjuster, and an OR gate.

The truncated multiplier produces  $U'$  which satisfies the following inequalities.

$$U - 2^{-l} < U' \leq U \quad (2)$$

The normalizer normalizes  $U'$  and produces  $V'$  ( $= [1.v'_1 \dots v'_l]$ ) as formula (1). The rounding bit generator calculates  $r'$  as described in the previous section according to the rounding mode. Incrementer<sub>m</sub> sums up rounding bit  $r'$  and  $V'$ , and produces  $W'$ .  $W'$  may be different from  $W$ . The adjuster generates the result  $W'' (= [w''_{-1}w''_0.w''_1 \dots w''_l])$  from  $W'$  and the least significant bit of  $Z_m$ , i.e.,  $w_l$ , as follows:

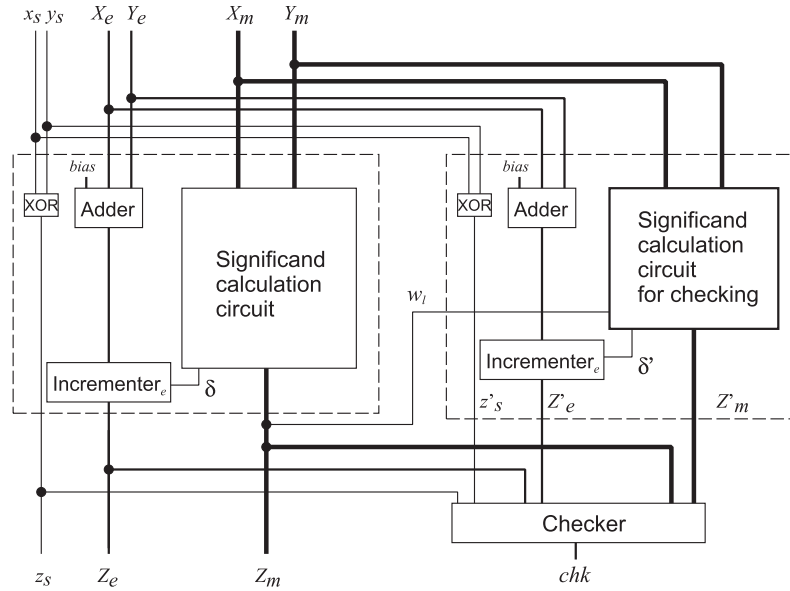


Fig. 1 Floating-point multiplier with concurrent error detection capability by partial duplication

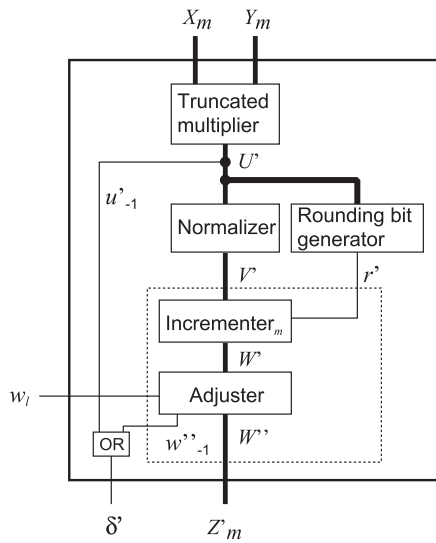


Fig. 2 Significand calculation circuit for checking

gardless of the rounding mode because of inequalities (2). Therefore, we can obtain the adjusted result by incrementing  $W'$  when the least significant bits of  $W$  and  $W'$  are not the same.

We use the least significant bit of  $Z_m$ , i.e.,  $w_l$ , for adjusting the output of the truncated multiplier. The multiplier may not detect an erroneous significand output only when  $w_l$  is inverted by an error because the adjuster generates the same output to the incorrect  $Z_m$ . In other words, it detects any erroneous significand if it has an error larger than 1 ulp. Note that, when  $w_l$  is inverted by an error, the erroneous one is chosen for  $W''$ . In this case, the both inputs of the checker are erroneous. Even though the output of the normal significand calculation circuit has error of 1 ulp, the checker detects the error if the polarity of the two 1 ulp errors is different, i.e., one of the checker inputs is 1 ulp larger and the other is 1 ulp smaller than the correct result. Therefore, half cases of 1 ulp error of the final result are detected by the checker.

$$W'' = \begin{cases} W' & (\text{if } w_l = w'_l) \\ W' + 2^{-l} & (\text{otherwise}) \end{cases}$$

where  $w'_l$  is the least significant bit of  $W'$ . If no error exists,  $W''$  is the same as  $W$ . The fraction part of significand  $Z'_m$  for checking is obtained as

$$Z'_m = [.w''_1 \cdots w''_l].$$

The significand calculation circuit sends increment  $\delta' (= u'_{-1} \vee w'_{-1})$  to the exponent sub-circuit for checking. The normal result, i.e.,  $z_s, z_e$ , and  $Z_m$ , and the output from the circuit for checking, i.e.,  $z'_s, z'_e$ , and  $Z'_m$ , are compared by the checker.

Note that the adjuster works appropriately with any rounding mode.  $W$  is equal to either  $W'$  or  $W' + 2^{-l}$  re-

### 3.3 A Design Consideration of the Significand Calculation Circuit for Checking

We consider design of the significand calculation circuit for checking in detail.

We show an example of the part of partial product bits for a truncated multiplier for single-precision in Fig. 3. A dot represents a partial product bit. Every output value of a truncated multiplier for single-precision, which sums up the dots surrounded by the broken lines, satisfies inequalities (2) where  $l = 23$ . The truncated multiplier for double-precision can be designed in a similar way. Because the truncated multiplier sums up fewer bits than the normal one, it performs calculation in shorter time and occupies smaller circuit area. Note that, the delay of the overall circuit is longer

than the normal significant calculation circuit because the checker output is obtained after two outputs.

We can shorten the critical path of the significant calculation circuit for checking by designing the part of the circuit surrounded by the broken lines in Fig. 2 cleverly. This part calculates  $W''$  according to the values of  $r'$ ,  $w_l$ , and  $v'_l$  as follows:

$$W'' = \begin{cases} V' & (\text{if } r' = 0 \wedge w_l = v'_l) \\ V' + 2^{-l+1} & (\text{if } r' = 1 \wedge w_l = v'_l) \\ V' + 2^{-l} & (\text{otherwise}). \end{cases} \quad (3)$$

When  $V' + 2^{-l+1}$  is represented as  $T' = [t'_{-1}t'_{-2} \cdots t'_1]$ ,  $V' + 2^{-l}$  can be obtained from  $V'$  or  $T'$  as follows:

$$V' + 2^{-l} = \begin{cases} [t'_{-1}t'_{-2} \cdots t'_1 0] & (\text{if } v'_l = 1) \\ [1.v'_1 \cdots v'_{l-1} 1] & (\text{otherwise}). \end{cases} \quad (4)$$

From (3) and (4), we can obtain  $W''$  as follows:

$$W'' = \begin{cases} [t'_{-1}t'_{-2} \cdots t'_1 w_l] & (\text{if } sel_{Z'} = 1) \\ [01.v'_1 v'_2 \cdots v'_{l-1} w_l] & (\text{otherwise}) \end{cases}$$

where  $sel_{Z'} = (\overline{w_l} \wedge v'_l) \vee (v'_l \wedge r') \vee (r' \wedge \overline{w_l})$ . Therefore, we can design this part as shown in Fig. 4. The design includes only one incrementer, Incrementer<sub>m</sub>, that calculates  $V' + 2^{-l+1}$ . Note that a naive design includes two incrementers. Though signal  $w_l$  is fed from the output of the normal circuit,

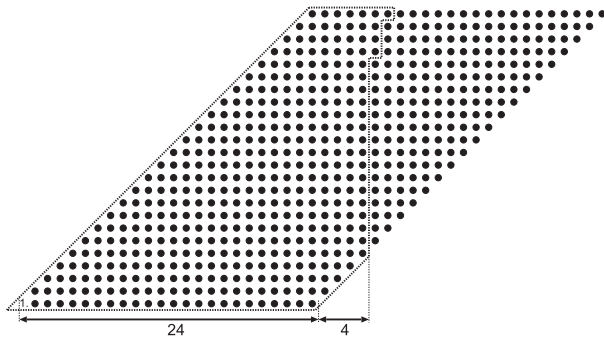


Fig. 3 Example of partial product bits for a truncated multiplier in a single-precision multiplier

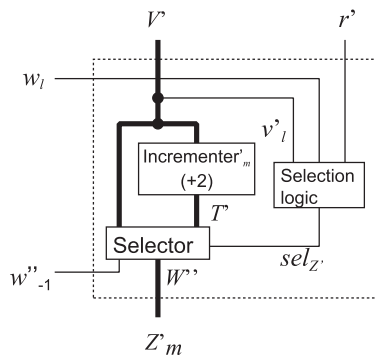


Fig. 4 Alternative design of Incrementer<sub>m</sub> and Adjuster for the significant calculation circuit for checking

influence of this part to the circuit delay of the overall circuit is small because output delay of an integer multiplier and an incrementer is not uniform at all positions, and the value of  $w_l$  is obtained earlier than the value of the latest delayed position generally.

#### 4. Evaluation

We estimated the circuit area, and evaluated the error detection ratio and several metrics about error detection of the proposed floating-point multiplier. For comparison, we considered three other multipliers: a fully duplicated multiplier and two multipliers using residue checking based on [9]. For the circuits using residue checking, we chose 3 or 15 as the modulus. Modulo-3 checking is used widely [10], [17], and modulo-15 checking is also used in IBM z196 microprocessor [10], [18]. We used duplication for checking of the sign bit and the exponent for all the four multipliers to evaluate error detectability and area of the significant calculation circuits fairly. We used the design in Sect. 3.3 for the proposed multiplier. We used a two-rail checker as the checker.

We used Synopsys design compiler with NanGate

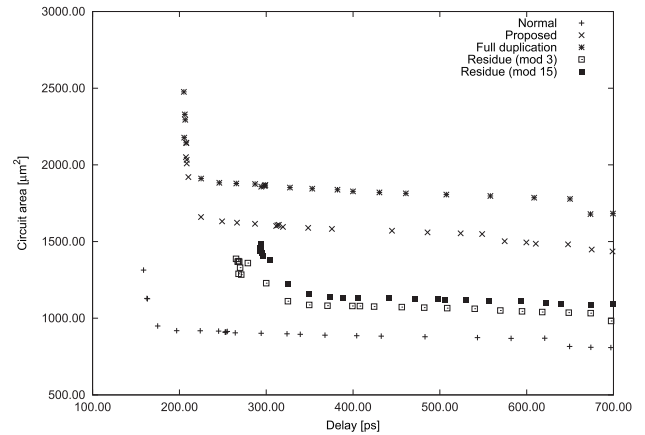


Fig. 5 Circuit area and delay time of single-precision floating-point multiplier designs

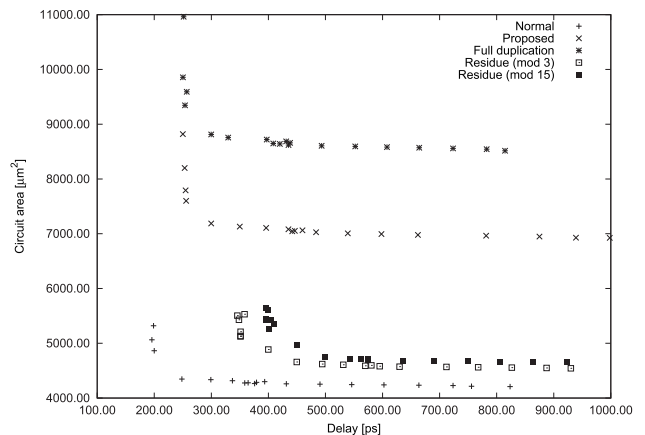


Fig. 6 Circuit area and delay time of double-precision floating-point multiplier designs



**Table 1** Area overhead of floating-point multipliers

	Single-precision (delay: 300 ps)		Double-precision (delay: 400 ps)	
	Area [ $\mu\text{m}^2$ ]	Overhead [%]	Area [ $\mu\text{m}^2$ ]	Overhead [%]
Normal	910.3	-	4298.4	-
Proposed	1615.5	77.5	7106.2	65.3
Full duplication	1875.1	105.9	8719.1	102.8
Residue (mod 3)	1228.8	35.0	4885.7	13.7
Residue (mod 15)	1379.1	51.5	5344.6	24.3

**Table 2** Evaluation results of error detections

	Error detection ratio [%]	Average magnitude of overlooked error [ulp]	Ratio of errors in exponent bits [%]	FP ratio [%]
Proposed	91.2	1 (exact)	0.0 (no error)	55.1
Full duplication	100.0 (no error)	0 (no error)	-	54.1
Residue (mod 3)	98.7	119545	9.1	52.7
Residue (mod 15)	99.2	5275	28.0	57.5

15nm open cell library [19] to synthesize the designs. We synthesized the designs with various timing constraints. Figures 5 and 6 show circuit area of single-precision designs and double-precision ones, respectively. Horizontal axis denotes delay time of the designs and vertical axis denotes circuit area. In the figures, “Normal” denotes the multiplier without error detection capability, “Proposed” denotes the proposed multiplier, “Full duplication” denotes the multiplier using full duplication, and “Residue (mod 3)” and “Residue (mod 15)” denote the multipliers using residue checking. The figures show that the proposed multiplier has shorter delay time compared with the multipliers using residue checking. Residue checking is timing-critical because residue generation is necessary after calculation of the normal result and the output for checking. In the figures, the shortest delay of the proposed multiplier is almost the same as that of the full duplication. The adjuster parts of the proposed multiplier have small influence to the circuit delay.

The circuit area and the area overhead are shown in Table 1. We show the estimation of single-precision designs synthesized with 300 ps delay constraint and double-precision designs synthesized with 400 ps delay constraint. The area overhead of the proposed multiplier is about 78% for the single-precision design and about 65% for the double-precision design. The area overhead is smaller compared with that of the multiplier using full duplication.

We evaluated the error detection ratio and other metrics about error detection of the four multipliers. We considered error caused by a single stuck-at fault for evaluation. We used Synopsys TetraMax for simulation of the multipliers inserting a stuck-at fault. We carried out simulation for single-precision multipliers synthesized with 300 ps delay constraint with 50,000 random patterns for every single stuck-at fault. The results are shown in Table 2.

The fault detection ratio of the proposed multiplier is over 90%. The magnitude of any overlooked error of the proposed multiplier is exactly 1 ulp. It is very small against the average magnitude of overlooked error of the multipliers using residue checking.

We show the ratio of erroneous outputs whose exponent bits are erroneous in all overlooked ones. The ratio for

the proposed multiplier is 0%. The multiplier has two increment signals  $\delta$  and  $\delta'$  for the two exponent sub-circuits and erroneous outputs caused by erroneous incrementation on one of the two signals can be detected. On the other hand, the ratios for the multipliers using residue checking are over 9%.

We also evaluated the fault positive ratio (FP ratio) which is the ratio of correct outputs when the checker indicates error. Results of the four multipliers are almost the same.

## 5. Conclusion

We have proposed a floating-point multiplier with concurrent error detection capability by partial duplication. It detects any erroneous output with magnitude of error larger than 1 ulp which may be overlooked by residue checking. It works appropriately with any rounding mode defined in IEEE 754 floating-point standard. Area overhead of the proposed multiplier is small compared with the multiplier using full duplication.

The proposed multiplier utilizes the idea of tolerating overlooked small errors, considering the nature of floating-point multiplication. Further researches about trade-off between area overhead and magnitude of detectable error will be interesting.

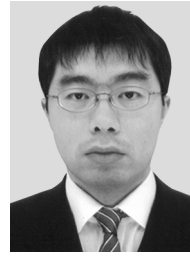
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